

## 2.9 Logarithmic Expressions

AP Precalculus

## 2.9 Practice Solutions

**Directions: Rewrite the following logarithms as exponents.**

1)  $\log_2 64 = 6$

$$2^6 = 64$$

2)  $\log_4 \frac{1}{64} = -3$

$$4^{-3} = \frac{1}{64}$$

3)  $\log_{25} 125 = \frac{3}{2}$

$$25^{\frac{3}{2}} = 125$$

**Directions: Rewrite the following exponents as logarithms.**

4)  $10^3 = 1000$

$$\log 1000 = 3$$

5)  $16^{\frac{5}{2}} = 1024$

$$\log_{16} 1024 = \frac{5}{2}$$

6)  $10^{-2} = \frac{1}{100}$

$$\log \frac{1}{100} = -2$$

**Directions: WITHOUT using a CALCULATOR, find the value of logarithm.**

7)  $\log_5 625 = x$

$$5^x = 625$$

$$5^x = 5^4$$

$$x = 4$$

8)  $\log 100,000 = x$

$$10^x = 100,000$$

$$10^x = 10^5$$

$$x = 5$$

9)  $\log_{27} 81 = x$

$$27^x = 81$$

$$3^{3x} = 3^4$$

$$3x = 4$$

$$x = \frac{4}{3}$$

**Directions: Use a CALCULATOR to find the value of logarithm. Round to three decimal places.**

10)  $\log 140$

$$2.146$$

11)  $\log_9 120$

$$2.179$$

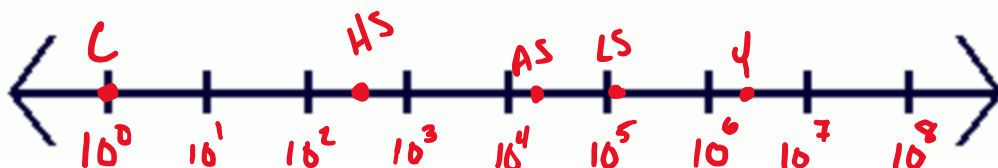
12)  $\log_3 18$

$$2.631$$

**Directions: For the given data construct a plot using a LOGARITHMIC scale using the given bases. Be sure to label your axis.**

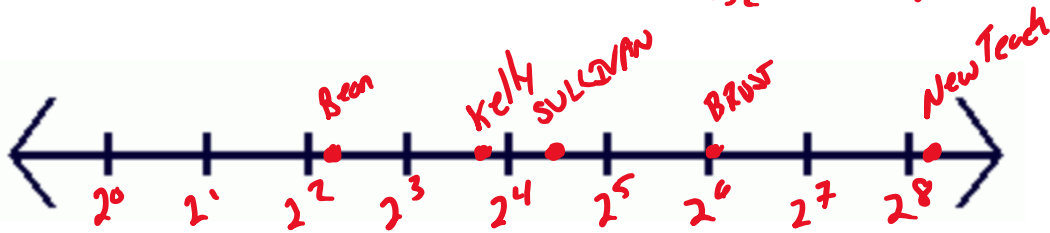
12) Logarithmic Scale of base 10.

Person	Midichlorians Found in Cells
Chewbacca	1 $\log 1 = 0$
Han Solo	330 $\log 330 = 2.519$
Luke Skywalker	125,000 $\log 125,000 = 5.097$
Yoda	2,750,000 $\log 2,750,000 = 6.439$
Anakin Skywalker	20,000 $\log 20,000 = 4.3$



### 13) Logarithmic Scale of Base 2

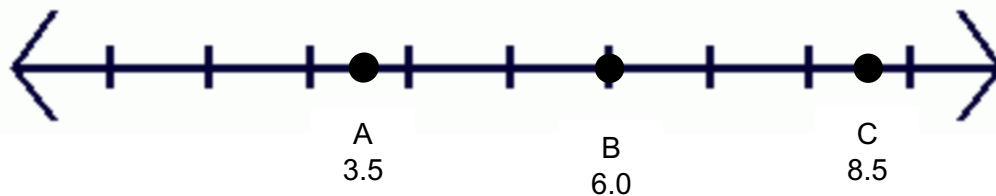
Person	Errors Per Section
Bean	5 $\log_2 5 = 2.232$
Brust	68 $\log_2 68 = 6.087$
Sullivan	24 $\log_2 24 = 4.585$
Kelly	15 $\log_2 15 = 3.907$
New Teacher	300 $\log_2 300 = 8.229$



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## 2.9 Test Prep

The Richter Scale is a common way of measuring earthquakes around the world. The scale measures the amplitude of the waves from the seismic activity. The Richter Scale uses a logarithmic scale of base 10. Since it uses this scale it means that each order of magnitude is 10 times greater than the previous one. So a 6.0 earthquake is ten times intense then a 5.0 earthquake.



14. Which statements most accurately describes how much more intense Earthquake C was than Earthquake A.

- a. Earthquake C is 5 times more intense.
- b. Earthquake C is  $5 \times 10$  or 50 times more intense.
- c. Earthquake C is  $10^5$  or 100,000 more intense.
- d. Earthquake C is log 5 times more intense.

$8.5 - 3.5 = 5$   
 BUT IT IS 10 times more for each  
 so its  $10 \cdot 10 \cdot 10 \cdot 10 \cdot 10$   
 or  $10^5 = 100,000$

15. Which of the following statements is true.

- a. The increase in intensity from Earthquake A to B is greater than the increase in intensity from Earthquake B to C.
- b. The increase in intensity from Earthquake A to B is less than the increase in intensity from Earthquake B to C.
- c. Earthquake B is as many times more intense to Earthquake A, as Earthquake C is as many times more intense to Earthquake B.

$A \rightarrow B$   
 $6 - 3.5 = 2.5$   
 so  $10^{2.5}$

$B \rightarrow C$   
 $8.5 - 6.0 = 2.5$   
 so  $10^{2.5}$