

1.9 Rational Functions & Vertical Asymptotes

AP Precalculus

Name: _____

Find the vertical asymptote(s) of the following rational functions, if one exists.

1.

$$f(x) = \frac{x^2 - 4}{x^2 - 8x - 20}$$

2.

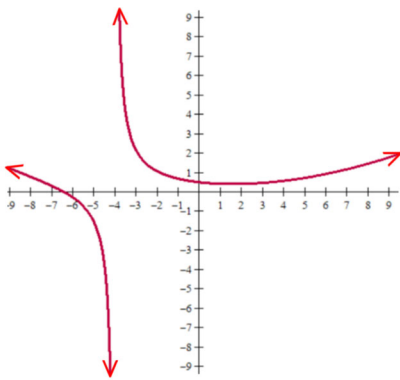
$$g(x) = \frac{x^2 + 3x}{x^2 - 9x + 18}$$

3.

$$h(t) = \frac{t^2 - 2t - 48}{t^2 + 12t + 36}$$

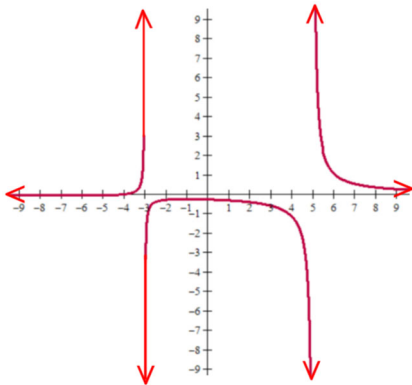
Use the graph of f to find the vertical asymptote(s). Use limit notation.

4.



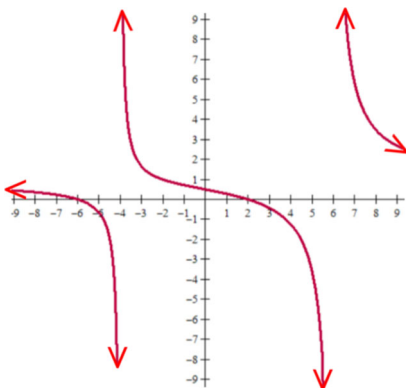
Limit Notation Vertical Asymptote(s):

5.



Limit Notation Vertical Asymptote(s):

6.



Limit Notation Vertical Asymptote(s):

CALCULATOR ACTIVE Complete the table to answer the following.

7. $f(x) = \frac{x+5}{x-2}$

x	1.9	1.99	1.999	2	2.001	2.01	2.1
$f(x)$							

Vertical Asymptote:

Limit Notation of Vertical Asymptote:

CALCULATOR ACTIVE Complete the table to answer the following.

8. $f(x) = \frac{x^3+8}{x^2+3x}$

x	-3.1	-3.01	-3.001	-3	-2.999	-2.99	-2.9
$f(x)$							

Vertical Asymptote:

Limit Notation of Vertical Asymptote:

Answers to 1.9 CA #1

1. $x = 10$	2. $x = 3$ and 6	3. $t = -6$																															
4. $\lim_{x \rightarrow -4^-} f(x) = -\infty$ and $\lim_{x \rightarrow -4^+} f(x) = \infty$	5. $\lim_{x \rightarrow -3^-} f(x) = \infty$ and $\lim_{x \rightarrow -3^+} f(x) = -\infty$ $\lim_{x \rightarrow 5^-} f(x) = -\infty$ and $\lim_{x \rightarrow 5^+} f(x) = \infty$	6. $\lim_{x \rightarrow -4^-} f(x) = -\infty$ and $\lim_{x \rightarrow -4^+} f(x) = \infty$ $\lim_{x \rightarrow 6^-} f(x) = -\infty$ and $\lim_{x \rightarrow 6^+} f(x) = \infty$																															
7. <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><th>x</th><th>$f(x)$</th></tr> <tr><td>1.9</td><td>-69</td></tr> <tr><td>1.99</td><td>-699</td></tr> <tr><td>1.999</td><td>-6999</td></tr> <tr><td>2</td><td>undefined</td></tr> <tr><td>2.001</td><td>7001</td></tr> <tr><td>2.01</td><td>701</td></tr> <tr><td>2.1</td><td>71</td></tr> </table> <p style="text-align: center;">vertical asymptote: $x = 2$ $\lim_{x \rightarrow 2^-} f(x) = -\infty$ $\lim_{x \rightarrow 2^+} f(x) = \infty$</p>	x	$f(x)$	1.9	-69	1.99	-699	1.999	-6999	2	undefined	2.001	7001	2.01	701	2.1	71	8. <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><th>x</th><th>$f(x)$</th></tr> <tr><td>-3.1</td><td>-70.29</td></tr> <tr><td>-3.01</td><td>-640.2</td></tr> <tr><td>-3.001</td><td>-6340</td></tr> <tr><td>-3</td><td>undefined</td></tr> <tr><td>-2.999</td><td>6326.4</td></tr> <tr><td>-2.99</td><td>626.45</td></tr> <tr><td>-2.9</td><td>56.51</td></tr> </table> <p style="text-align: center;">vertical asymptote: $x = -3$ $\lim_{x \rightarrow -3^-} f(x) = -\infty$ $\lim_{x \rightarrow -3^+} f(x) = \infty$</p>	x	$f(x)$	-3.1	-70.29	-3.01	-640.2	-3.001	-6340	-3	undefined	-2.999	6326.4	-2.99	626.45	-2.9	56.51
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