### 3.4 Sine and Cosine Function Graphs <br> AP Precalculus

1. We are given an angle $\theta$, in standard position as shown in the figure. The function $g$ is given by $g(a)=\cos a$. For the angle $\alpha$ (not shown), $\theta<\alpha<\frac{3 \pi}{2}$. Which of the following is true?

(A) $g(\alpha)<g(\theta)$
(B) $g(\alpha)>g(\theta)$
(C) $g(\alpha)=g(\theta)$
(D) Depending on the value of $\alpha$, sometimes $g(\alpha)<g(\theta)$ and sometimes
 $g(\alpha)>g(\theta)$.
2. We are given an angle $\theta$, in standard position as shown in the figure. The function $g$ is given by $g(a)=\sin a$. For the angle $\alpha$ (not shown), $\theta<\alpha<2 \pi$. Which of the following is true?
$B$
(A) $g(\alpha)<g(\theta)$
(B) $g(\alpha)>g(\theta)$
(C) $g(\alpha)=g(\theta)$
(D) Depending on the value of $\alpha$, sometimes $g(\alpha)<g(\theta)$ and sometimes $g(\alpha)>g(\theta)$.

3. We are given an angle $\theta$, in standard position as shown in the figure. The function $g$ is given by $g(a)=\cos a$. For the angle $\alpha$ (not shown), $\theta<\alpha<2 \pi$. Which of the following is true?
D
(A) $g(\alpha)<g(\theta)$
(B) $g(\alpha)>g(\theta)$
(C) $g(\alpha)=g(\theta)$
(D) Depending on the value of $\alpha$, sometimes $g(\alpha)<g(\theta)$ and sometimes $g(\alpha)>g(\theta)$.


The function $f$ is given by $f(\theta)=\cos \theta$. Describe the concavity of $f$ on the interval, and if $f$ is increasing or decreasing on the interval.
4. $0<\theta<\frac{\pi}{2}$

5. $\frac{\pi}{2}<\theta<\pi$

6. $\pi<\theta<\frac{3 \pi}{2}$

Concave up
Increasing
7. $\frac{3 \pi}{2}<\theta<2 \pi$

Concave down
Increasing
8. $0<\theta<\pi$

Concave down from $0<\theta<\frac{\pi}{2}$
Concave up from $\frac{\pi}{2}<\theta<\pi$
Decreasing from $0<\boldsymbol{\theta}<\boldsymbol{\pi}$

The function $f$ is given by $f(\theta)=\sin \theta$. Describe the concavity of $f$ on the interval, and if $f$ is increasing or decreasing on the interval.
9. $0<\theta<\frac{\pi}{2}$
10. $\frac{\pi}{2}<\theta<\pi$


| Concave down <br> Decreasing |
| :--- |
| $13 . \pi<\theta<2 \pi$ |

11. $\pi<\theta<\frac{3 \pi}{2}$
12. $\frac{3 \pi}{2}<\theta<2 \pi$

## Concave up

Decreasing

| Concave up |
| :---: |
| Increasing |

$$
\begin{aligned}
& \text { Concave up from } \pi<\theta<2 \pi \\
& \text { Decreasing from } \pi<\theta<\frac{3 \pi}{2} \\
& \text { Increasing from } \frac{3 \pi}{2}<\theta<2 \pi
\end{aligned}
$$

### 3.4 Sine and Cosine Function Graphs

### 3.4 Test Prep

14. For the function $f(\theta)=\cos \theta$, what are all values of the domain when $f(\theta)=1$ ?

## $2 n \pi$ where $n$ in an integer.

15. For the function $g(\theta)=\sin \theta$, what are all values of the domain when $g(\theta)=0$ ?

## $n \boldsymbol{\pi}$ where $\boldsymbol{n}$ in an integer.

