

## 2.14 Logarithmic Function Context and Data Modeling

AP Precalculus

Name: \_\_\_\_\_

CA #2

**Instructions: Use the information given to answer the questions. Round to nearest thousandth.**

- 1) Mr. Kelly opens a bank account that pays interest compounded continuously when his son was born. He put \$5,000 in right away as well. He knows that he can calculate the value of the account by using the formula,  $A(t) = Pe^{rt}$ , where  $A(t)$  is the amount in the account after  $t$  years, and  $P$  is the initial amount invested and  $r$  is the rate earned.
  - a) Mr. Kelly is hoping that by the time his son is 18 there will be \$25,000 in the account. What rate would the account need to be compounded at for that to happen?
  - b) How much money would be in the account if Mr. Kelly's son didn't touch the money until he was 65 years old for his retirement and earned 8.3% interest?

**Instructions: Use the data provided to find a regression equation and answer the questions.**

- 1) Scientists take a sample from a local river and study how many bacteria are in each sample. They've been taking data for several years and want to find a regression equation that models the number of bacteria found (in thousands) as a function of the number of years.

Year	1	3	5	8
Bacteria (in thousands)	14.3	52.4	70.3	86.8

- a) What's a logarithmic regression equation that could model this situation?
- b) How many years until there are 100 thousand bacteria in a sample on the beach?
- c) How many bacteria can be found in a sample after 15 years?

- 2) Scientists are worried about the cardinal population in Northeast Ohio. Each year they measured the number of tagged cardinals. They hope to find a regression equation that models the number of cardinals as a function of how many years has passed.

Year	3	4	8	9
# of Cardinals	1090	1061	992	980

- a) What's a logarithmic regression equation that could model this situation?
- b) How many cardinals can we predict there will be in year 20?
- c) How many years for there to be 800 cardinals for the year?

#### ANSWERS

- 1) A) 16.05%  
B) \$1,101,510.74
- 2) A)  $f(x) = 14.234 + 34.854 \ln x$   
B)  $x = 11.7$ , year 12.  
C) 108.620 thousand bacteria
- 3) A)  $f(x) = 1199.725 - 99.962 \ln x$   
B) 900 cardinals  
C) 55 years