

# 1.7A Rational Functions and End Behavior

AP Precalculus

Name: \_\_\_\_\_

**CA #1**

**State the domain of the following rational functions. Use interval notation.**

1.  $f(x) = \frac{x^3+1}{x^2-16}$

Domain:

2.  $h(x) = \frac{x+3}{2x^2+10x-28}$

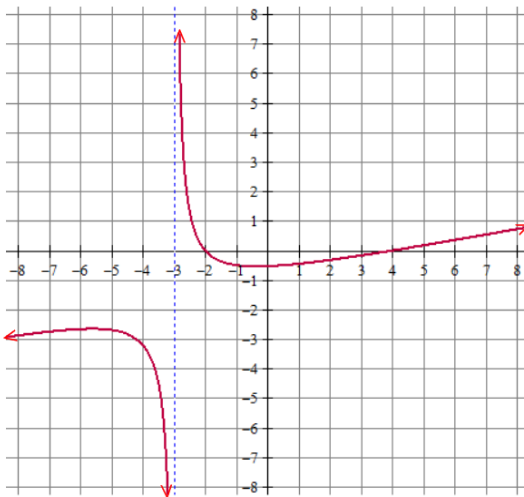
Domain:

3.  $d(t) = \frac{t^2-3t+1}{4-3t}$

Domain:

**Use the graph of the rational function  $f$  to find the following.**

4.

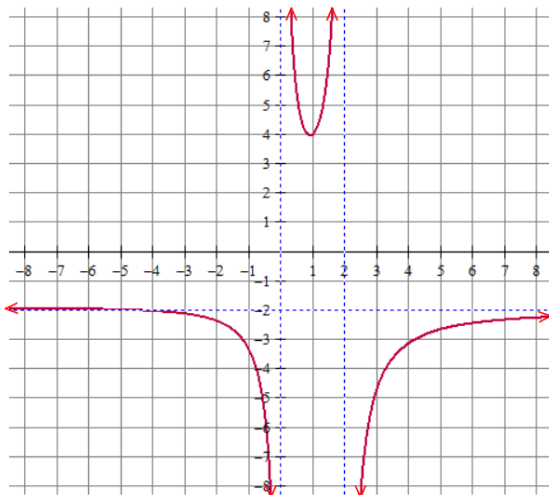


Domain:

End Behavior:

Is there horizontal asymptote?  
If so, write the equation of the horizontal asymptote.

5.



Domain:

End Behavior:

Is there horizontal asymptote?  
If so, write the equation of the horizontal asymptote.

Continued on the back.

**CALCULATOR ACTIVE Complete the table to answer the following.**

6.  $f(x) = \frac{x^2}{x^2 - 4x}$

$x$	-10,000	-1,000	-100	100	1,000	10,000
$f(x)$						

End Behavior:

Is there horizontal asymptote?

If so, write the equation of the horizontal asymptote.

7.  $d(t) = \frac{t^3 - 3t}{2t + 1}$

$t$	-5,000	-500	-50	50	500	5,000
$d(t)$						

End Behavior:

Is there horizontal asymptote?

If so, write the equation of the horizontal asymptote.

**Answers to 1.7A CA #1**

1. $(-\infty, -4) \cup (-4, 4) \cup (4, \infty)$	6.	<table border="1"> <tr> <th><math>x</math></th> <th><math>f(x)</math></th> </tr> <tr> <td>-10,000</td> <td>0.9996</td> </tr> <tr> <td>-1,000</td> <td>0.99602</td> </tr> <tr> <td>-100</td> <td>0.9615</td> </tr> <tr> <td>100</td> <td>1.0417</td> </tr> <tr> <td>1,000</td> <td>1.004</td> </tr> <tr> <td>10,000</td> <td>1.0004</td> </tr> </table>	$x$	$f(x)$	-10,000	0.9996	-1,000	0.99602	-100	0.9615	100	1.0417	1,000	1.004	10,000	1.0004	7.	<table border="1"> <tr> <th><math>t</math></th> <th><math>d(t)</math></th> </tr> <tr> <td>-5,000</td> <td><math>\approx 1.2 \times 10^7</math></td> </tr> <tr> <td>-500</td> <td>125124</td> </tr> <tr> <td>-50</td> <td>1261.1</td> </tr> <tr> <td>50</td> <td>1236.1</td> </tr> <tr> <td>500</td> <td>124874</td> </tr> <tr> <td>5,000</td> <td><math>\approx 1.2 \times 10^7</math></td> </tr> </table>	$t$	$d(t)$	-5,000	$\approx 1.2 \times 10^7$	-500	125124	-50	1261.1	50	1236.1	500	124874	5,000	$\approx 1.2 \times 10^7$
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5. Domain: $(-\infty, 0) \cup (0, 2) \cup (2, \infty)$ End Behavior: $\lim_{x \rightarrow -\infty} f(x) = -2$ and $\lim_{x \rightarrow \infty} f(x) = -2$ Horizontal Asymptote: $y = -2$		$\lim_{x \rightarrow -\infty} f(x) = 1$ $\lim_{x \rightarrow \infty} f(x) = 1$ HA: $y = 1$	$\lim_{t \rightarrow -\infty} f(x) = \infty$ $\lim_{t \rightarrow \infty} f(x) = \infty$ HA: none																													