

Exponent Rules

RULE	Rewrite using rational exponents.		
$\sqrt[3]{x^2} = x^{\frac{2}{3}}$	1. $\sqrt[5]{x^3}$ $x^{3/5}$	2. $\sqrt[3]{3^2}$ $3^{2/3}$	3. $\sqrt[3]{e^2}$ $e^{2/3}$

RULE	Rewrite without negative or rational exponents.		
$x^{-\frac{1}{2}} = \frac{1}{\sqrt{x}}$	1. $x^{\frac{1}{3}}$ $\sqrt[3]{x}$	2. 4^{-2} $\frac{1}{4^2} = \frac{1}{16}$	3. $e^{\frac{1}{2}}$ \sqrt{e}

RULE	Simplify.		
$x^2 \cdot x^3 = x^5$	1. $x^3 \cdot x^4$ x^7	2. $2^3 \cdot 2^x$ 2^{3+x}	3. $e^{3x}e^{2x}$ $e^{3x+2x} = e^{5x}$

RULE	Simplify.		
$\frac{x^2}{x^3} = x^{-1} = \frac{1}{x}$	1. $\frac{2^5}{2^7}$ $2^{5-7} = 2^{-2} = \frac{1}{2^2}$ $\frac{1}{4}$	2. $\frac{e^{3x}}{e^2}$ e^{3x-2}	3. $\frac{x^4}{\sqrt{x}} = \frac{x^4}{x^{1/2}}$ $x^{4-\frac{1}{2}} = x^{7/2} = \sqrt{x^7}$

RULE	Simplify.		
$(x^3)^2 = x^6$	1. $(2x^5)^3$ $2^3 x^{15}$ $8x^{15}$	2. $(4^x)^2$ 4^{2x}	3. $(\sqrt{e})^5$ $e^{5/2}$

Logarithmic Rules

RULE	Rewrite		
$a \log_b x = \log_b x^a$	1. $3 \log_5 x$ $\log_5 x^3$	2. $2 \log_7 e$ $\log_7 e^2$	3. $\frac{1}{2} \ln 4$ $\ln 4^{1/2} = \ln \sqrt{4}$ $\ln 2$

Logarithmic Rules

RULE	Rewrite		
$\log_b x + \log_b y = \log_b xy$	1. $\log_4 x + \log_4 5$ $\log_4 (5x)$	2. $\log e^2 + \log y^3$ $\log (e^2 y^3)$	3. $5 \ln 3 + \ln x$ $\ln 3^5 + \ln x$ $\ln (3^5 x)$

RULE	Condense		
$\log_b x - \log_b y = \log_b \frac{x}{y}$	1. $\log_4 (2x) - \log_4 (5)$ $\log_4 \left(\frac{2x}{5} \right)$	2. $\log e^x - \log x^3$ $\log \left(\frac{e^x}{x^3} \right)$	3. $2 \ln x - \ln x$ $\ln x^2 - \ln x$ $\ln \left(\frac{x^2}{x} \right) = \ln x$

CHANGE OF BASE	Change base to 3	Change base to 2	Change base to 10
$\log_b x = \frac{\log_c x}{\log_c b}$	1. $\log_2 x$ $\frac{\log_3 x}{\log_3 2}$	2. $\log_8 7$ $\frac{\log_2 7}{\log_2 8} = \frac{\log_2 7}{3}$ $\frac{1}{3} \log_2 7$	3. $\log_3 100$ $\frac{\log 100}{\log 3} = \frac{2}{\log 3}$

Trig Identities

Pythagorean:	Sum/Difference:	Double Angle:
$\sin^2 x + \cos^2 x = 1$ $\sin^2 x = 1 - \cos^2 x$ $\cos^2 x = 1 - \sin^2 x$ $1 + \cot^2 x = \csc^2 x$ $\tan^2 x + 1 = \sec^2 x$	$\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$ $\sin(\alpha - \beta) = \sin \alpha \cos \beta - \cos \alpha \sin \beta$ $\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$ $\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$	$\sin(2\alpha) = 2 \sin \alpha \cos \alpha$ $\cos(2\alpha) = \cos^2 \alpha - \sin^2 \alpha$ $= 1 - 2 \sin^2 \alpha$

TRIGONOMETRY

$\csc x = \frac{1}{\sin x}$	$\tan x = \frac{\sin x}{\cos x}$	
$\sec x = \frac{1}{\cos x}$	$\cot x = \frac{\cos x}{\sin x}$	
$\cot x = \frac{1}{\tan x}$	$\sin^{-1} x = \arcsin x$	

Free Response Question #4

AP Precalculus

PRACTICE

NO CALCULATOR – Answer the following practice FRQ #4 question. Grade using the scoring rubric.

1.

(A) The functions g and h are given by

$$4 = \log_3(2x - 5)$$

$$3^4 = 3^{\log_3(2x - 5)}$$

$$81 = 2x - 5$$

$$\frac{86}{2} = \frac{2x}{2}$$

$$43 = x$$

Solution 1 point

(B) The functions j and k are given by

domain: $\cos x \neq 0$ $j(x) = (\tan^2 x)(1 - \sin^2 x)$

$$j(x) = \tan^2 x (\cos^2 x)$$

$$j(x) = \frac{\sin^2 x}{\cos^2 x} \cdot \cos^2 x$$

$$j(x) = \sin^2 x$$

Expression 1 point

(C) The function m is given by

$$4 = 2 \cos(2x) + 3$$

$$\frac{1}{2} = \frac{2 \cos(2x)}{2}$$

$$\frac{1}{2} = \cos(2x)$$

$$\cos^{-1}\left(\frac{1}{2}\right) = \cos^{-1}(\cos(2x))$$

$$\frac{\pi}{3} = 2x$$

$$\frac{5\pi}{3} = 2x$$

One value of x 1 point

$$\frac{\pi}{4} = \sin^{-1}(6x)$$

$$\sin\left(\frac{\pi}{4}\right) = \sin(\sin^{-1}(6x))$$

$$\frac{\sqrt{2}}{2} = \frac{6x}{6}$$

$$\frac{\sqrt{2}}{12} = x$$

Solution 1 point

$$k(x) = \frac{e^{3x}(e^{2x})}{(\sqrt{e})^{6x}} = \frac{e^{5x}}{e^{6x}}$$

$$k(x) = e^{5x - 6x}$$

$$k(x) = e^{-x}$$

Expression 1 point

$$2x = \frac{\pi}{3} + 2\pi n$$

$$2x = \frac{5\pi}{3} + 2\pi n$$

$$x = \frac{\pi}{6} + \pi n$$

$$x = \frac{5\pi}{6} + \pi n$$

where n is an integer

All values of x 1 point

Your Score: ____ out of 6 points

Free Response Question #4

PRACTICE

AP Precalculus

NO CALCULATOR – Answer the following practice FRQ #4 question. Grade using the scoring rubric.

2.

(A) The functions g and h are given by

$$2e = e^{(x-2)} + e$$

$$\frac{-e}{e} = \frac{-e}{e}$$

$$e = e^{(x-2)}$$

$$\ln e = \ln e^{(x-2)}$$

$$1 = x - 2$$

$$\frac{+2}{+2} \quad \frac{+2}{+2}$$

$$3 = x$$

Solution 1 point

$$\frac{2\pi}{3} = \frac{3 \arccos(\pi x)}{3}$$

$$\frac{2\pi}{3} = \cos^{-1}(\pi x)$$

$$\cos\left(\frac{2\pi}{3}\right) = \cos(\cos^{-1}(\pi x))$$

$$-\frac{1}{2} = \frac{\pi x}{\pi}$$

$$-\frac{1}{2\pi} = x$$

Solution 1 point

(B) The functions j and k are given by

$$j(x) = \csc x - \sin x \quad \text{domain: } \sin x \neq 0$$

$$j(x) = \frac{1}{\sin x} - \sin x$$

$$j(x) = \frac{1}{\sin x} - \frac{\sin x \cdot \sin x}{1 \cdot \sin x}$$

$$j(x) = \frac{1}{\sin x} - \frac{\sin^2 x}{\sin x}$$

$$j(x) = \frac{1 - \sin^2 x}{\sin x}$$

$$j(x) = \frac{\cos^2 x}{\sin x}$$

$$j(x) = \frac{\cos x \cos x}{\sin x}$$

$$j(x) = \cot x \cos x$$

Expression 1 point

$$k(x) = 2 \ln(4x^2) - \frac{1}{2} \ln(4x^4) \quad \text{domain: } x > 0$$

$$k(x) = \ln(4x^2)^2 - \ln(4x^4)^{\frac{1}{2}}$$

$$k(x) = \ln(16x^4) - \ln \sqrt{4x^4}$$

$$k(x) = \ln(16x^4) - \ln(2x^2)$$

$$k(x) = \ln\left(\frac{16x^4}{2x^2}\right)$$

$$k(x) = \ln(8x^2)$$

Expression 1 point

(C) The function m is given by

$$0 = 2 \sin^2 x - \sin x$$

$$0 = \sin x (2 \sin x - 1)$$

$$\sin x = 0$$

$$x = \sin^{-1}(0)$$

$$x = 0 + \pi n$$

$$2 \sin x - 1 = 0$$

$$\frac{+1}{-1} \quad \frac{+1}{-1}$$

$$\frac{2 \sin x}{2} = \frac{1}{2}$$

$$\sin x = \frac{1}{2}$$

$$x = \sin^{-1}\left(\frac{1}{2}\right)$$

$$x = \frac{\pi}{6} \text{ and } \frac{5\pi}{6} + 2\pi n$$

One value of x 1 point

$$x = 0 + \pi n$$

$$x = \frac{\pi}{6} + 2\pi n$$

$$x = \frac{5\pi}{6} + 2\pi n$$

where n is an integer

All values of x 1 point

Your Score: ___ out of 6 points

Free Response Question #4

AP Precalculus

PRACTICE

NO CALCULATOR – Answer the following practice FRQ #4 question. Grade using the scoring rubric.

3.

(A) The functions g and h are given by

$$6 = \ln(x - 5) + 4$$

$$\begin{array}{ccc} & -4 & \\ & \underline{-4} & \end{array}$$

$$2 = \ln(x - 5)$$

$$e^2 = e^{\ln(x - 5)}$$

$$\begin{array}{ccc} e^2 & = & x - 5 \\ \underline{+5} & & \underline{+5} \end{array}$$

$$e^2 + 5 = x$$

Solution 1 point

$$\frac{-\pi}{4} = \frac{4 \arctan x}{4}$$

$$-\frac{\pi}{4} = \tan^{-1}(x)$$

$$\tan\left(-\frac{\pi}{4}\right) = \tan\left(\tan^{-1}(x)\right)$$

$$-1 = x$$

Solution 1 point

(B) The functions j and k are given by

domain: $\cos x \neq 0$ $j(x) = \frac{\sin(2x)}{2\cos(x)}$

$$j(x) = \frac{2 \sin x \cdot \cos x}{2 \cos x}$$

$$j(x) = \frac{\cancel{2} \sin x \cdot \cancel{\cos x}}{\cancel{2} \cos x}$$

$$j(x) = \sin x$$

Expression 1 point

$$k(x) = \frac{(4^{3x})(8^x)}{2}$$

$$k(x) = \frac{(2^2)^{3x} (2^3)^x}{2}$$

$$k(x) = \frac{2^{6x} \cdot 2^{3x}}{2}$$

$$k(x) = \frac{2^{9x}}{2^1}$$

$$k(x) = 2^{9x-1}$$

Expression 1 point

(C) The function m is given by

$$0 = 2e^{2x} - e^x$$

Factor out e^x

$$0 = e^x(2e^x - 1)$$

1 point

$e^x = 0$
Does not exist

$$2e^x - 1 = 0$$

$$\begin{array}{ccc} \underline{+1} & \underline{+1} & \\ 2e^x & = & 1 \\ \underline{\quad} & \underline{\quad} & \underline{\quad} \\ 2e^x & = & \frac{1}{2} \\ \underline{\quad} & \underline{\quad} & \underline{\quad} \\ e^x & = & \frac{1}{2} \end{array}$$

$$e^x = \frac{1}{2}$$

$$\ln e^x = \ln \frac{1}{2}$$

$$x = \ln \frac{1}{2}$$

Value of x 1 point

Your Score: _____ out of 6 points

Free Response Question #4

AP Precalculus

PRACTICE

NO CALCULATOR – Answer the following practice FRQ #4 question. Grade using the scoring rubric.

4.

(A) The functions g and h are given by

$$9 = 3^{(x-5)}$$

$$\log_3 9 = \log_3 3^{(x-5)}$$

$$\log_3 3^2 = x - 5$$

$$2 = x - 5$$

$$\begin{array}{r} +5 \\ \hline \end{array} \qquad \begin{array}{r} +5 \\ \hline \end{array}$$

$$7 = x$$

Solution 1 point

(B) The functions j and k are given by

domain: $\cos x \neq 0$
 $\sin x \neq 0$

$$j(x) = (1 + \tan^2 x)(\cot^2 x)$$

$$j(x) = \sec^2 x \cot^2 x$$

$$j(x) = \frac{1}{\cos^2 x} \cdot \frac{\cos^2 x}{\sin^2 x}$$

$$j(x) = \frac{1}{\sin^2 x}$$

$$j(x) = \csc^2 x$$

Expression 1 point

values of x in the interval of $[0, \pi]$

$$\cos x = (2\cos x)(\sin x)$$

$$\underline{-\cos x} \qquad \qquad \qquad \underline{-\cos x}$$

$$0 = 2\cos x \sin x - \cos x$$

$$0 = \cos x (2\sin x - 1)$$

$$\cos x = 0$$

$$x = \cos^{-1}(0)$$

$$x = \frac{\pi}{2} \quad \cancel{\frac{3\pi}{2}}$$

$$x = \frac{\pi}{2}, \frac{\pi}{6}, \text{ and } \frac{5\pi}{6}$$

Solution 1 point

$$2\sin x - 1 = 0$$

$$\begin{array}{r} +1 \quad +1 \\ \hline \end{array}$$

$$\frac{2\sin x}{2} = \frac{1}{2}$$

$$\sin x = \frac{1}{2}$$

$$x = \sin^{-1}(\frac{1}{2})$$

$$x = \frac{\pi}{6} \text{ and } \frac{5\pi}{6}$$

$$k(x) = \log_2(x+2) - 4\log_2(x) + \log_2(x^2) \quad \text{domain: } x > -2$$

$$k(x) = \log_2(x+2) - \log_2(x^4) + \log_2(x^2)$$

$$k(x) = \log_2\left(\frac{(x+2)(x^2)}{x^4}\right)$$

$$k(x) = \log_2\left(\frac{(x+2)x^2}{x^4}\right)$$

$$k(x) = \log_2\left(\frac{x+2}{x^2}\right)$$

Expression 1 point

(C) The function m is given by

$$\frac{2\pi}{3} = \sin^{-1}(\cos x) + \frac{\pi}{2}$$

$$\frac{2\pi}{3} - \frac{\pi}{2} = \sin^{-1}(\cos x)$$

$$\frac{\pi}{6} = \sin^{-1}(\cos x)$$

$$\sin\left(\frac{\pi}{6}\right) = \sin\left(\sin^{-1}(\cos x)\right)$$

$$\frac{1}{2} = \cos x$$

$$\cos^{-1}\left(\frac{1}{2}\right) = x$$

One value of x 1 point

$$x = \frac{\pi}{3} + 2\pi n$$

where n is

$$x = \frac{5\pi}{3} + 2\pi n$$

an integer

All values of x 1 point

Your Score: _____ out of 6 points