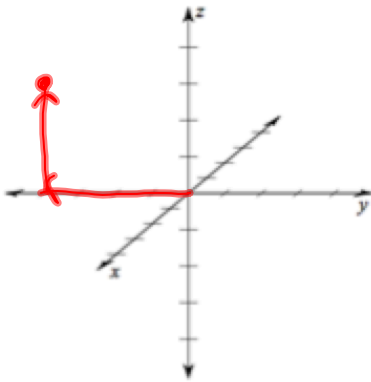


### 13.1 Three Dimensional Graphs

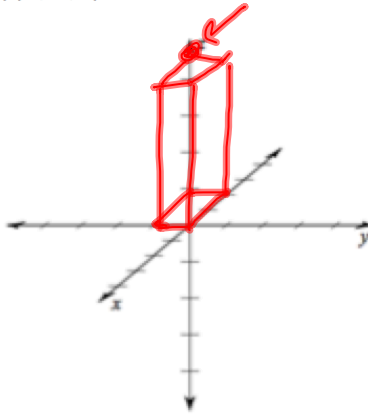
### PRACTICE

Directions: Plot each given point. Make sure you show how you got to your point.

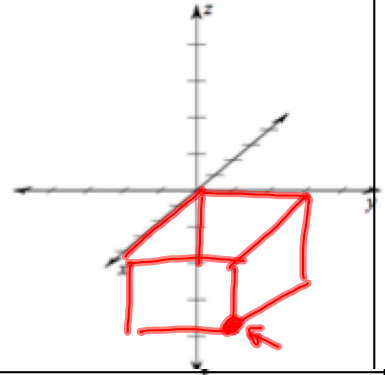
1) (0, -4, 3)



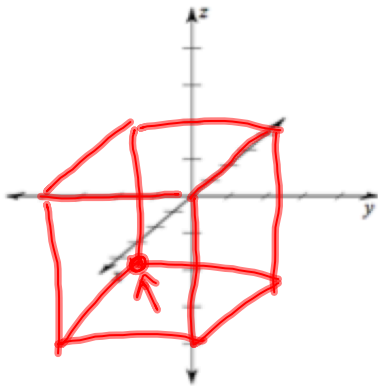
2) (-2, -1, 4)



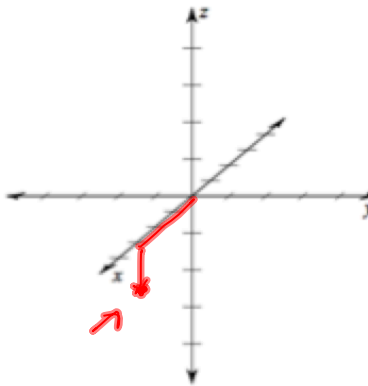
3) (4, 3, -2)



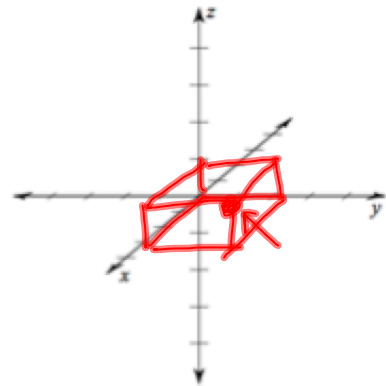
4) (-4, -4, -4)



5) (3, 0, -1)



6) (3, 2, 1)



Directions: Find the distance and midpoint for each.

7) (5, 0, 12) and (-4, 8, -2)

$$\sqrt{(-4-5)^2 + (0-8)^2 + (12-(-2))^2}$$

$$\sqrt{(-9)^2 + (-8)^2 + 14^2}$$

$$\sqrt{341}$$

$$\approx 18.47$$

$$\left\{ \frac{5+(-4)}{2}, \frac{0+8}{2}, \frac{12+(-2)}{2} \right\}$$

$$\left\{ \frac{1}{2}, 4, 5 \right\}$$

8) (-7, 3, 4) and (-3, 8, -9)

$$\sqrt{(-7-(-3))^2 + (3-8)^2 + (4-(-9))^2}$$

$$\sqrt{(-4)^2 + (-5)^2 + (13)^2}$$

$$\sqrt{210}$$

$$\approx 14.49$$

$$\left\{ \frac{-7+(-3)}{2}, \frac{3+8}{2}, \frac{4+(-9)}{2} \right\}$$

$$\left\{ -5, \frac{11}{2}, -\frac{5}{2} \right\}$$

9) (-4, -4, -4) and (10, 0, -2)

$$\sqrt{(-4-10)^2 + (-4-0)^2 + (-4-(-2))^2}$$

$$\sqrt{(-14)^2 + (-4)^2 + (-2)^2}$$

$$\sqrt{216} \approx 14.7$$

$$\left\{ \frac{-4+10}{2}, \frac{-4+0}{2}, \frac{-4+(-2)}{2} \right\}$$

$$\left\{ 3, -2, -3 \right\}$$

10) (4, 9, 2) and (-4, -9, -2)

$$\sqrt{(4-(-4))^2 + (9-(-9))^2 + (2-(-2))^2}$$

$$\sqrt{8^2 + 18^2 + 4^2}$$

$$\sqrt{404} \approx 20.10$$

$$\left\{ \frac{4+(-4)}{2}, \frac{9+(-9)}{2}, \frac{2+(-2)}{2} \right\}$$

$$\left\{ 0, 0, 0 \right\}$$

11) (15, -2, 6) and (-5, 8, 0)

$$\sqrt{(15 - (-5))^2 + (-2 - 8)^2 + (6 - 0)^2}$$

$$\sqrt{20^2 + (-10)^2 + 6^2}$$

$$\sqrt{536} \approx 23.15$$

$$\left( \frac{15 + (-5)}{2}, \frac{-2 + 8}{2}, \frac{6 + 0}{2} \right)$$

$$(5, 3, 3)$$

12) (-5, -6, -7) and (0, 0, 6)

$$\sqrt{(-5 - 0)^2 + (-6 - 0)^2 + (-7 - 6)^2}$$

$$\sqrt{(-5)^2 + (-6)^2 + (-13)^2}$$

$$\sqrt{230} \approx 15.17$$

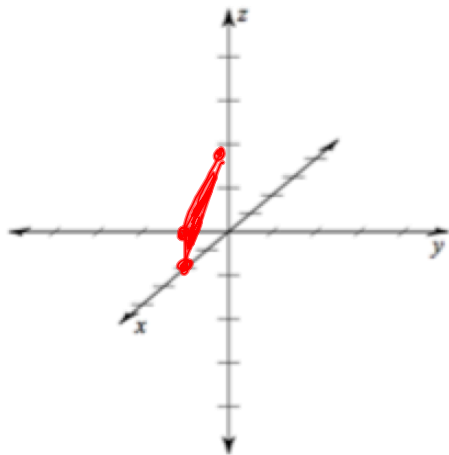
$$\left( \frac{-5 + 0}{2}, \frac{-6 + 0}{2}, \frac{-7 + 6}{2} \right)$$

$$\left( -\frac{5}{2}, -3, -\frac{1}{2} \right)$$

Directions: Find the intercepts and graph the equation.

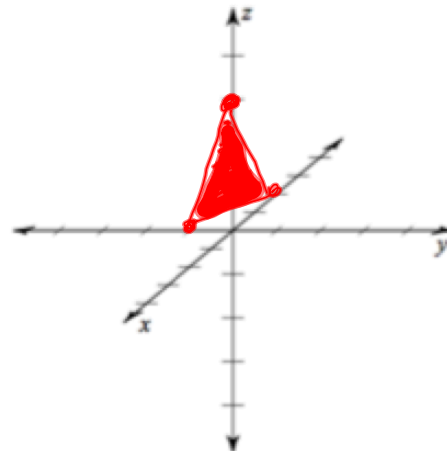
13)  $x - 2y + z = 2$

$$\begin{cases} x = 2 \\ -2y = 2 \\ z = 2 \end{cases} \Rightarrow \begin{cases} y = -1 \\ z = 2 \end{cases}$$



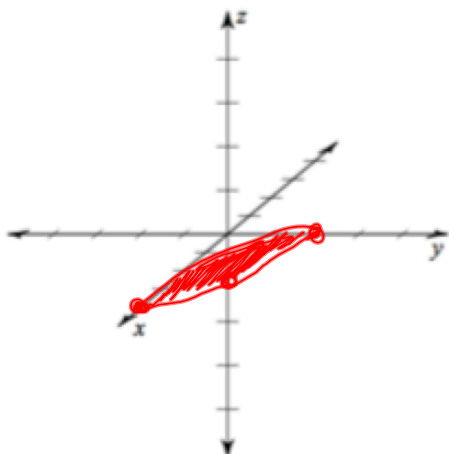
14)  $3x + 6y - 2z = -6$

$$\begin{cases} 3x = -6 \\ 6y = -6 \\ -2z = -6 \end{cases} \Rightarrow \begin{cases} x = -2 \\ y = -1 \\ z = 3 \end{cases}$$



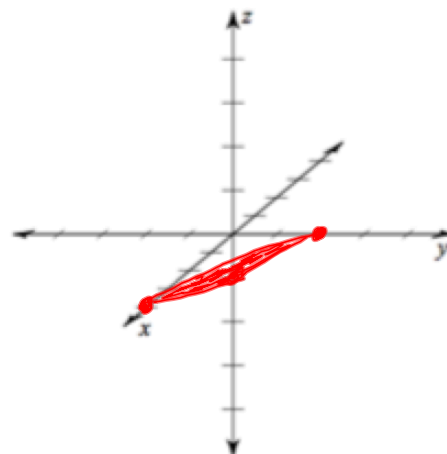
15)  $x + 4y - 8z = 8$

$$\begin{cases} x = 8 \\ 4y = 8 \\ -8z = 8 \end{cases} \Rightarrow \begin{cases} y = 2 \\ z = -1 \end{cases}$$



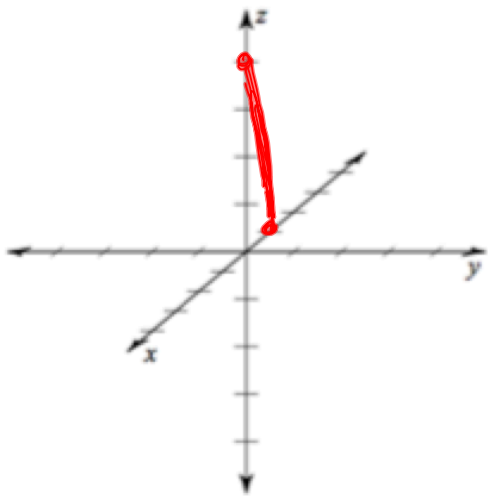
16)  $5x + 10y - 20z = 20$

$$\begin{cases} 5x = 20 \\ 10y = 20 \\ -20z = 20 \end{cases} \Rightarrow \begin{cases} x = 4 \\ y = 2 \\ z = -1 \end{cases}$$



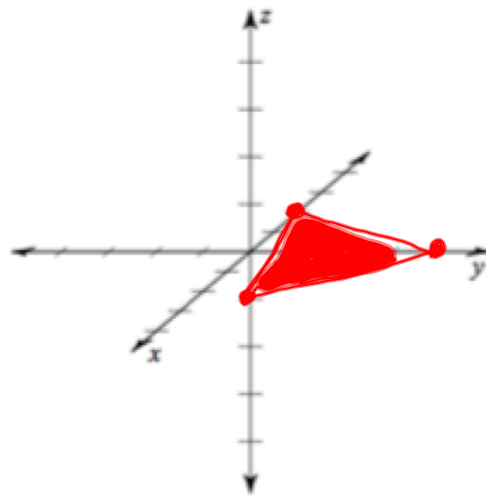
17)  $8x - 2z = -8$

$8x = -8 \mid -2z = -8$   
 $x = -1 \mid z = 4$



18)  $32x - 16y + 64z = -64$

$32x = -64 \mid -16y = -64 \mid 64z = -64$   
 $x = -2 \mid y = 4 \mid z = -1$



REVIEW SKILLZ

Find the next two terms and describe how the sequence is derived.

1)  $\frac{2}{9}, \frac{2}{3}, 2, 6, 18, 54, 162$

Multiply the previous term by 3

2)  $2, -4, 8, -16, 32, -64$

Multiply the previous term by -2.

3)  $1, -1, -3, -5, -7, -9$

Subtract the previous term by 2.